QuCumber Documentation

Release v1.0.0

PIQuIL

2018-12-30

Introduction

1	Installation 1.1 Github 1.2 Windows 1.3 Linux / MacOS	1 1 1 1
2	Theory	3
3	Download the tutorials	5
4	Training	7
5	Training	13
6	Sampling and calculating observables 6.1 Generate new samples 6.2 Calculate an observable using the Observable module 6.2.1 Custom observable 6.2.2 TFIM Energy 6.2.3 Adding observables 6.2.4 Template for your custom observable	19 19 20 20 22 23 23
7	Training while monitoring observables	25
8	RBM	29
9	Quantum States 9.1 Positive WaveFunction 9.2 Complex WaveFunction 9.3 Abstract WaveFunction	31 31 35 38
10	Callbacks	43
11	Observables 11.1 Pauli Operators 11.2 Neighbour Interactions 11.3 Abstract Observable	49 49 53 54
12	Complex Algebra	22

13 Data Handling	59
14 Indices and tables	61
Python Module Index	63

Installation

QuCumber only supports Python 3, not Python 2. If you are using Python 2, please update! You will also want to install the following packages, if you have not already.

- 1. Pytorch v0.4.1 (https://pytorch.org/)
- 2. tqdm (https://github.com/tqdm/tqdm)

1.1 Github

Navigate to the qucumber page on github (https://github.com/PIQuIL/QuCumber) and clone the repository by typing:

```
git clone https://github.com/PIQuIL/QuCumber.git
```

Navigate to the main directory and type:

python setup.py install

1.2 Windows

Navigate to the directory (through command prompt) where pip.exe is installed (usually C:\Python\Scripts\pip.exe) and type:

```
pip.exe install qucumber
```

1.3 Linux / MacOS

Open up a terminal, then type:

pip install qucumber

Theory

For a basic introduction to Restricted Boltzmann Machines, click here.

Download the tutorials

Once you have installed QuCumber, we recommend going through our tutorial that is divided into two parts.

- 1. Training a wave function to reconstruct a positive-real wave function (i.e. no phase) from a transverse-field Ising model (TFIM) and then generating new data.
- 2. Training an wave function to reconstruct a complex wave function (i.e. with a phase) from a simple two qubit random state and then generating new data.

We have made interactive python notebooks that can be downloaded (along with the data required) here. Note that the linked examples are from the most recent stable release (relative to the version of the docs you're currently viewing), and may not match the examples shown in the following pages. It is recommended that you refer to documentation for the latest stable release: https://qucumber.readthedocs.io/en/stable/.

If you wish to simply view the static, non-interactive notebooks, continue to the next page of the documentation.

Alternatively, you can view interactive notebooks online at: launch binder, though they may be slow.

```
[ ]: import numpy as np
import matplotlib.pyplot as plt
from qucumber.nn_states import PositiveWaveFunction
from qucumber.callbacks import MetricEvaluator
import qucumber.utils.training_statistics as ts
import qucumber.utils.data as data
```

The Python class *PositiveWaveFunction* contains generic properties of a RBM meant to reconstruct a positive-real wavefunction, the most notable one being the gradient function required for stochastic gradient descent.

To instantiate a *PositiveWaveFunction* object, one needs to specify the number of visible and hidden units in the RBM. The number of visible units, *num_visible*, is given by the size of the physical system, i.e. the number of spins or qubits (10 in this case), while the number of hidden units, *num_hidden*, can be varied to change the expressiveness of the neural network.

Note: The optimal *num_hidden* : *num_visible* ratio will depend on the system. For the TFIM, having this ratio be equal to 1 leads to good results with reasonable computational effort.

Training

To evaluate the training in real time, the fidelity between the true ground-state wavefunction of the system and the wavefunction that qucumber reconstructs, $|\langle \psi | \psi_{RBM} \rangle|^2$, will be calculated along with the Kullback-Leibler (KL) divergence (the RBM's cost function). It will also be shown that any custom function can be used to evaluate the training.

First, the training data and the true wavefunction of this system must be loaded using the data utility.

```
[ ]: psi_path = "tfimld_psi.txt"
    train_path = "tfimld_data.txt"
    train_data, true_psi = data.load_data(train_path, psi_path)
```

As previously mentioned, to instantiate a *PositiveWaveFunction* object, one needs to specify the number of visible and hidden units in the RBM. These two quantities equal will be kept equal.

```
[]: nv = train_data.shape[-1]
nh = nv
nn_state = PositiveWaveFunction(num_visible=nv, num_hidden=nh)
# nn_state = PositiveWaveFunction(num_visible=nv, num_hidden=nh, gpu = False)
```

By default, qucumber will attempt to run on a GPU if one is available (if one is not available, qucumber will default to CPU). If one wishes to run qucumber on a CPU, add the flag "gpu = False" in the *PositiveWaveFunction* object instantiation (i.e. uncomment the line above).

Now the hyperparameters of the training process can be specified.

- 1. epochs: the total number of training cycles that will be performed (default = 100)
- 2. **pos_batch_size**: the number of data points used in the positive phase of the gradient (default = 100)
- 3. **neg_batch_size**: the number of data points used in the negative phase of the gradient (default = *pos_batch_size*)
- 4. **k**: the number of contrastive divergence steps (default = 1)
- 5. **Ir**: the learning rate (default = 0.001)

Note: For more information on the hyperparameters above, it is strongly encouraged that the user to read through the brief, but thorough theory document on RBMs located in the qucumber documentation. One does not have to specify these hyperparameters, as their default values will be used without the user overwriting them. It is recommended to keep with the default values until the user has a stronger grasp on what these hyperparameters mean. The quality and the computational efficiency of the training will highly depend on the choice of hyperparameters. As such, playing around with the hyperparameters is almost always necessary.

For the TFIM with 10 sites, the following hyperparameters give excellent results.

```
[ ]: epochs = 500
    pbs = 100    # pos_batch_size
    nbs = 200    # neg_batch_size
    lr = 0.01
    k = 10
```

For evaluating the training in real time, the *MetricEvaluator* will be called in order to calculate the training evaluators every 100 epochs. The *MetricEvaluator* requires the following arguments.

- 1. **log_every**: the frequency of the training evaluators being calculated is controlled by the *log_every* argument (e.g. *log_every* = 200 means that the *MetricEvaluator* will update the user every 200 epochs)
- 2. A dictionary of functions you would like to reference to evaluate the training (arguments required for these functions are keyword arguments placed after the dictionary)

The following additional arguments are needed to calculate the fidelity and KL divergence in the *training_statistics* utility.

- target_psi: the true wavefunction of the system
- space: the hilbert space of the system

The training evaluators can be printed out via the verbose=True statement.

Although the fidelity and KL divergence are excellent training evaluators, they are not practical to calculate in most cases; the user may not have access to the target wavefunction of the system, nor may generating the hilbert space of the system be computationally feasible. However, evaluating the training in real time is extremely convenient.

Any custom function that the user would like to use to evaluate the training can be given to the *MetricEvaluator*, thus avoiding having to calculate fidelity and/or KL divergence. Any custom function given to *MetricEvaluator* must take the neural-network state (in this case, the *PositiveWaveFunction* object) and keyword arguments. As an example, the function to be passed to the *MetricEvaluator* will be the fifth coefficient of the reconstructed wavefunction multiplied by a parameter, *A*.

```
[ ]: def psi_coefficient(nn_state, space, A, **kwargs):
    norm = nn_state.compute_normalization(space).sqrt_()
    return A * nn_state.psi(space)[0][4] / norm
```

Now the hilbert space of the system can be generated for the fidelity and KL divergence and the dictionary of functions the user would like to compute every "*log_every*" epochs can be given to the *MetricEvaluator*.

```
[ ]: log_every = 10
space = nn_state.generate_hilbert_space(nv)
```

Now the training can begin. The *PositiveWaveFunction* object has a property called *fit* which takes care of this. *MetricEvaluator* must be passed to the *fit* function in a list (*callbacks*).

```
[ ]: callbacks = [
    MetricEvaluator(
        log_every,
        {"Fidelity": ts.fidelity, "KL": ts.KL, "A_\Prbm_5": psi_coefficient},
```

(continues on next page)

(continued from previous page)

```
target_psi=true_psi,
verbose=True,
space=space,
A=3.,
)
]
nn_state.fit(
train_data,
epochs=epochs,
pos_batch_size=pbs,
neg_batch_size=nbs,
lr=lr,
k=k,
callbacks=callbacks,
)
# nn_state.fit(train_data, callbacks=callbacks)
```

All of these training evaluators can be accessed after the training has completed, as well. The code below shows this, along with plots of each training evaluator versus the training cycle number (epoch).

```
[]: fidelities = callbacks[0].Fidelity
    KLs = callbacks[0].KL
    coeffs = callbacks[0].A_\Psirbm_5
    # Please note that the key given to the *MetricEvaluator* must be what comes after_
    \hookrightarrow callbacks[0].
    epoch = np.arange(log_every, epochs + 1, log_every)
[]: # Some parameters to make the plots look nice
    params = { 'text.usetex': True,
                 'font.family': 'serif',
                 'legend.fontsize': 14,
                 'figure.figsize': (10, 3),
                 'axes.labelsize': 16,
                 'xtick.labelsize':14,
                 'vtick.labelsize':14.
                 'lines.linewidth':2,
                 'lines.markeredgewidth': 0.8,
                 'lines.markersize': 5,
                 'lines.marker': "o",
                 "patch.edgecolor": "black"
              }
    plt.rcParams.update(params)
    plt.style.use('seaborn-deep')
[]: # Plotting
    fig, axs = plt.subplots(nrows=1, ncols=3, figsize=(14, 3))
    ax = axs[0]
    ax.plot(epoch, fidelities, "o", color = "CO", markeredgecolor="black")
    ax.set_ylabel(r'Fidelity')
    ax.set_xlabel(r'Epoch')
    ax = axs[1]
    ax.plot(epoch, KLs, "o", color = "C1", markeredgecolor="black")
    ax.set_ylabel(r'KL Divergence')
    ax.set_xlabel(r'Epoch')
                                                                                 (continues on next page)
```

(continued from previous page)

```
ax = axs[2]
ax.plot(epoch, coeffs, "o", color = "C2", markeredgecolor="black")
ax.set_ylabel(r'$A\psi_{RBM}[5]$')
ax.set_xlabel(r'Epoch')
plt.tight_layout()
plt.savefig("fid_KL.pdf")
plt.show()
```

It should be noted that one could have just ran *nn_state.fit(train_samples)* and just used the default hyperparameters and no training evaluators.

To demonstrate how important it is to find the optimal hyperparameters for a certain system, restart this notebook and comment out the original *fit* statement and uncomment the one below. The default hyperparameters will be used instead. Using the non-default hyperparameters yielded a fidelity of approximately 0.994, while the default hyperparameters yielded a fidelity of approximately 0.523!

The RBM's parameters will also be saved for future use in other tutorials. They can be saved to a pickle file with the name "saved_params.pt" with the code below.

```
[]: nn_state.save("saved_params.pt")
```

This saves the weights, visible biases and hidden biases as torch tensors with the following keys: "weights", "visible_bias", "hidden_bias".

```
[ ]: import numpy as np
import torch
import matplotlib.pyplot as plt
from qucumber.nn_states import ComplexWaveFunction
from qucumber.callbacks import MetricEvaluator
import qucumber.utils.unitaries as unitaries
import qucumber.utils.cplx as cplx
import qucumber.utils.training_statistics as ts
import qucumber.utils.data as data
```

The Python class *ComplexWaveFunction* contains generic properties of a RBM meant to reconstruct a complex wavefunction, the most notable one being the gradient function required for stochastic gradient descent.

To instantiate a *ComplexWaveFunction* object, one needs to specify the number of visible and hidden units in the RBM. The number of visible units, *num_visible*, is given by the size of the physical system, i.e. the number of spins or qubits (2 in this case), while the number of hidden units, *num_hidden*, can be varied to change the expressiveness of the neural network.

Note: The optimal *num_hidden* : *num_visible* ratio will depend on the system. For the two-qubit wavefunction described above, good results are yielded when this ratio is 1.

On top of needing the number of visible and hidden units, a *ComplexWaveFunction* object requires the user to input a dictionary containing the unitary operators (2x2) that will be used to rotate the qubits in and out of the computational basis, Z, during the training process. The *unitaries* utility will take care of creating this dictionary.

The *MetricEvaluator* class and *training_statistics* utility are built-in amenities that will allow the user to evaluate the training in real time.

Lastly, the *cplx* utility allows qucumber to be able to handle complex numbers. Currently, Pytorch does not support complex numbers.

Training

To evaluate the training in real time, the fidelity between the true wavefunction of the system and the wavefunction that qucumber reconstructs, $|\langle \psi | \psi_{RBM} \rangle|^2$, will be calculated along with the Kullback-Leibler (KL) divergence (the RBM's cost function). First, the training data and the true wavefunction of this system need to be loaded using the *data* utility.

```
[]: train_path = "qubits_train.txt"
    train_bases_path = "qubits_train_bases.txt"
    psi_path = "qubits_psi.txt"
    bases_path = "qubits_bases.txt"
    train_samples, true_psi, train_bases, bases = data.load_data(
        train_path, psi_path, train_bases_path, bases_path
)
```

The file *qubits_bases.txt* contains every unique basis in the *qubits_train_bases.txt* file. Calculation of the full KL divergence in every basis requires the user to specify each unique basis.

As previouosly mentioned, a *ComplexWaveFunction* object requires a dictionary that contains the unitarily operators that will be used to rotate the qubits in and out of the computational basis, Z, during the training process. In the case of the provided dataset, the unitaries required are the well-known H, and K gates. The dictionary needed can be created with the following command.

If the user wishes to add their own unitary operators from their experiment to *unitary_dict*, uncomment the block above. When *unitaries.create_dict()* is called, it will contain the identity and the H and K gates by default with the keys "Z", "X" and "Y", respectively.

The number of visible units in the RBM is equal to the number of qubits. The number of hidden units will also be taken to be the number of visible units.

By default, qucumber will attempt to run on a GPU if one is available (if one is not available, qucumber will default to CPU). If one wishes to run qucumber on a CPU, add the flag "gpu = False" in the *ComplexWaveFunction* object instantiation. Uncomment the line above to run this tutorial on a GPU.

Now the hyperparameters of the training process can be specified.

- 1. epochs: the total number of training cycles that will be performed (default = 100)
- 2. pos_batch_size: the number of data points used in the positive phase of the gradient (default = 100)
- 3. neg_batch_size: the number of data points used in the negative phase of the gradient (default = pos_batch_size)
- 4. **k**: the number of contrastive divergence steps (default = 1)
- 5. **Ir**: the learning rate (default = 0.001)

Note: For more information on the hyperparameters above, it is strongly encouraged that the user to read through the brief, but thorough theory document on RBMs. One does not have to specify these hyperparameters, as their default values will be used without the user overwriting them. It is recommended to keep with the default values until the user has a stronger grasp on what these hyperparameters mean. The quality and the computational efficiency of the training will highly depend on the choice of hyperparameters. As such, playing around with the hyperparameters is almost always necessary.

The two-qubit example in this tutorial should be extremely easy to train, regardless of the choice of hyperparameters. However, the hyperparameters below will be used.

```
[ ]: epochs = 100
    pbs = 50  # pos_batch_size
    nbs = 50  # neg_batch_size
    lr = 0.1
    k = 5
```

For evaluating the training in real time, the *MetricEvaluator* will be called to calculate the training evaluators every 10 epochs. The *MetricEvaluator* requires the following arguments.

- 1. **log_every**: the frequency of the training evaluators being calculated is controlled by the *log_every* argument (e.g. *log_every* = 200 means that the *MetricEvaluator* will update the user every 200 epochs)
- 2. A dictionary of functions you would like to reference to evaluate the training (arguments required for these functions are keyword arguments placed after the dictionary)

The following additional arguments are needed to calculate the fidelity and KL divergence in the *training_statistics* utility.

- target_psi (the true wavefunction of the system)
- **space** (the hilbert space of the system)

The training evaluators can be printed out via the verbose=True statement.

Although the fidelity and KL divergence are excellent training evaluators, they are not practical to calculate in most cases; the user may not have access to the target wavefunction of the system, nor may generating the hilbert space of the system be computationally feasible. However, evaluating the training in real time is extremely convenient.

Any custom function that the user would like to use to evaluate the training can be given to the *MetricEvaluator*, thus avoiding having to calculate fidelity and/or KL divergence. As an example, functions that calculate the the norm of each of the reconstructed wavefunction's coefficients are presented. Any custom function given to *MetricEvaluator* must take the neural-network state (in this case, the *ComplexWaveFunction* object) and keyword arguments. Although the given example requires the hilbert space to be computed, the scope of the *MetricEvaluator*'s ability to be able to handle any function should still be evident.

```
[]: def alpha(nn_state, space, **kwargs):
        rbm_psi = nn_state.psi(space)
        normalization = nn_state.compute_normalization(space).sqrt_()
        alpha_ = cplx.norm(
            torch.tensor([rbm_psi[0][0], rbm_psi[1][0]], device=nn_state.device)
             / normalization
        )
        return alpha_
    def beta(nn_state, space, **kwargs):
        rbm_psi = nn_state.psi(space)
        normalization = nn_state.compute_normalization(space).sqrt_()
        beta_ = cplx.norm(
            torch.tensor([rbm_psi[0][1], rbm_psi[1][1]], device=nn_state.device)
            / normalization
        )
        return beta
    def gamma(nn_state, space, **kwargs):
        rbm_psi = nn_state.psi(space)
        normalization = nn_state.compute_normalization(space).sqrt_()
        gamma_ = cplx.norm(
            torch.tensor([rbm_psi[0][2], rbm_psi[1][2]], device=nn_state.device)
            / normalization
        )
        return gamma_
    def delta(nn_state, space, **kwargs):
        rbm_psi = nn_state.psi(space)
        normalization = nn_state.compute_normalization(space).sqrt_()
        delta_ = cplx.norm(
            torch.tensor([rbm_psi[0][3], rbm_psi[1][3]], device=nn_state.device)
             / normalization
        )
        return delta_
```

Now the hilbert space of the system must be generated for the fidelity and KL divergence and the dictionary of functions the user would like to compute every "*log_every*" epochs must be given to the *MetricEvaluator*.

```
[ ]: log_every = 2
space = nn_state.generate_hilbert_space(nv)
callbacks = [
```

(continues on next page)

(continued from previous page)

```
MetricEvaluator(
         log_every,
         {
             "Fidelity": ts.fidelity,
             "KL": ts.KL,
             "norm\alpha": alpha,
               "norm\beta": beta,
#
#
                "normy": gamma,
#
                "norm\delta": delta,
         },
         target_psi=true_psi,
         bases=bases,
         verbose=True,
         space=space,
    )
]
```

Now the training can begin. The ComplexWaveFunction object has a property called *fit* which takes care of this.

```
[]: nn_state.fit(
    train_samples,
    epochs=epochs,
    pos_batch_size=pbs,
    neg_batch_size=nbs,
    lr=lr,
    k=k,
    input_bases=train_bases,
    callbacks=callbacks,
)
```

All of these training evaluators can be accessed after the training has completed, as well. The code below shows this, along with plots of each training evaluator versus the training cycle number (epoch).

```
[]: fidelities = callbacks[0].Fidelity
    KLs = callbacks[0].KL
    coeffs = callbacks[0].norm\alpha
     # Please note that the key given to the *MetricEvaluator* must be what comes after.
     \hookrightarrow callbacks[0].
    epoch = np.arange(log_every, epochs + 1, log_every)
[]: # Some parameters to make the plots look nice
    params = { 'text.usetex': True,
                 'font.family': 'serif',
                 'legend.fontsize': 14,
                 'figure.figsize': (10, 3),
                 'axes.labelsize': 16,
                 'xtick.labelsize':14,
                 'ytick.labelsize':14,
                 'lines.linewidth':2,
                 'lines.markeredgewidth': 0.8,
                 'lines.markersize': 5,
                 'lines.marker': "o",
                 "patch.edgecolor": "black"
              }
    plt.rcParams.update(params)
    plt.style.use('seaborn-deep')
```

```
[]: fig, axs = plt.subplots(nrows=1, ncols=3, figsize=(14, 3))
    ax = axs[0]
    ax.plot(epoch, fidelities, "o", color = "CO", markeredgecolor="black")
    ax.set_ylabel(r'Fidelity')
    ax.set_xlabel(r'Epoch')
    ax = axs[1]
    ax.plot(epoch, KLs, "o", color = "C1", markeredgecolor="black")
    ax.set_ylabel(r'KL Divergence')
    ax.set_xlabel(r'Epoch')
    ax = axs[2]
    ax.plot(epoch, coeffs, "o", color = "C2", markeredgecolor="black")
    ax.set_ylabel(r'$\vert\alpha\vert$')
    ax.set_xlabel(r'Epoch')
    plt.tight_layout()
    plt.savefig("complex_fid_KL.pdf")
    plt.show()
```

It should be noted that one could have just ran *nn_state.fit(train_samples)* and just used the default hyperparameters and no training evaluators.

At the end of the training process, the network parameters (the weights, visible biases and hidden biases) are stored in the *ComplexWaveFunction* object. One can save them to a pickle file, which will be called *saved_params.pt*, with the following command.

```
[ ]: nn_state.save("saved_params.pt")
```

This saves the weights, visible biases and hidden biases as torch tensors with the following keys: "weights", "visible_bias", "hidden_bias".

Sampling and calculating observables

6.1 Generate new samples

Firstly, to generate meaningful data, an RBM needs to be trained. Please refer to the tutorials 1 and 2 on training an RBM if how to train an RBM using qucumber is unclear. An RBM with a positive-real wavefunction describing a transverse-field Ising model (TFIM) with 10 sites has already been trained in the first tutorial, with the parameters of the machine saved here as *saved_params.pt*. The *autoload* function can be employed here to instantiate the corresponding *PositiveWaveFunction* object from the saved RBM parameters.

```
[]: import numpy as np
import matplotlib.pyplot as plt
from qucumber.nn_states import PositiveWaveFunction
from qucumber.observables import ObservableBase
import quantum_ising_chain
from quantum_ising_chain import TFIMChainEnergy
nn state = PositiveWaveFunction.autoload("saved_params.pt")
```

A PositiveWaveFunction object has a property called sample that takes in the following arguments.

- 1. k: the number of Gibbs steps to perform to generate the new samples
- 2. num_samples: the number of new data points to be generated

```
[ ]: new_samples = nn_state.sample(k=100, num_samples=10000)
print(new_samples)
```

With the newly generated samples, the user can now easily calculate observables that do not require any details associated with the RBM. A great example of this is the magnetization. To calculate the magnetization, the newly-generated samples must be converted to ± 1 from 1 and 0, respectively. The function below does the trick.

```
[ ]: def to_pml(samples):
    return samples.mul(2.).sub(1.)
```

Now, the magnetization is calculated as follows.

```
[ ]: def Magnetization(samples):
    return to_pml(samples).mean(1).abs().mean()
magnetization = Magnetization(new_samples).item()
print("Magnetization = %.5f" % magnetization)
```

The exact value for the magnetization is 0.5610.

The magnetization and the newly-generated samples can also be saved to a pickle file along with the RBM parameters in the *PositiveWaveFunction* object.

```
[]: nn_state.save(
    "saved_params_and_new_data.pt",
    metadata={"samples": new_samples, "magnetization": magnetization},
)
```

The *metadata* argument in the *save* function takes in a dictionary of data that you would like to save on top of the RBM parameters.

6.2 Calculate an observable using the Observable module

6.2.1 Custom observable

Qucumber has a built-in module called *Observable* which makes it easy for the user to compute any arbitrary observable from the RBM. To see the the *Observable* module in action, an example observable called *PIQuIL*, which inherits properties from the *Observable* module, is shown below.

The *PIQuIL* observable takes an σ^z measurement at a site and multiplies it by the measurement two sites from it. There is also a parameter, *P*, that determines the strength of each of these interactions. For example, for the dataset (-1, 1, 1, -1), (1, 1, 1, 1) and (1, 1, -1, 1) with P = 2, the *PIQuIL* for each data point would be $(2(-1 \times 1) + 2(1 \times -1) = -4), (2(1 \times 1) + 2(1 \times 1) = 4)$ and $(2(1 \times -1) + 2(1 \times 1) = 0)$, respectively.

```
[ ]: class PIQuIL(ObservableBase):
    def __init__(self, P):
        super(PIQuIL, self).__init__()
        self.P = P
    # Required : function that calculates the PIQuIL. Must be named "apply"
    def apply(self, nn_state, samples):
        to_pml(samples)
        interaction_ = 0
        for i in range(samples.shape[-1]):
            if (i + 3) > samples.shape[-1]:
                continue
        else:
                interaction_ += self.P * samples[:, i] * samples[:, i + 2]
        return interaction_
```

(continues on next page)

(continued from previous page)

P = 0.05 piquil = PIQuIL(P)

The *apply* function is contained in the *Observable* module, but is overwritten here. The *apply* function in *Observable* will compute the observable itself and must take in the RBM (*nn_state*) and a batch of samples as arguments. Thus, any new class inheriting from *Observables* that the user would like to define must contain a function called *apply* that calculates this new observable.

Although the *PIQuIL* observable could technically be computed without the use of the *Observable* module since it does not ever use the RBM (*nn_state*), it is still nonetheless a constructive example.

The real power in the *Observable* module is in the ability for the user to easily compute statistics of the observable from the generated sample. Since we have already generated new samples of data, the *PIQuIL* observable's mean, standard error and variance on the new data can be calculated with the *statistics_from_samples* function in the *Observable* module. The user must simply give the RBM and the samples as arguments.

[]: piquil_stats1 = piquil.statistics_from_samples(nn_state, new_samples)

The *statistics_from_samples* function returns a dictionary containing the mean, standard error and the variance with the keys "mean", "std_error" and "variance", respectively.

```
[]: print(
    "Mean PIQuIL: %.4f" % piquil_stats1["mean"], "+/- %.4f" % piquil_stats1["std_error
    +"]
)
print("Variance: %.4f" % piquil_stats1["variance"])
```

However, if the user did not have samples generated already, that is no problem. The *statistics* function in the *Observable* module will generate new samples internally and compute the mean, standard error and variance on those samples. Since the samples are not an argument in the *statistics* function, the user must now give the following additional arguments to the *statistics* function to generate the new samples.

- num_samples: the number of samples to generate internally
- **num_chains**: the number of Markov chains to run in parallel (default = 0)
- **burn_in**: the number of Gibbs steps to perform before recording any samples (default = 1000)
- **steps**: the number of Gibbs steps to perform between each sample (default = 1)

The *statistics* function will also return a dictionary containing the mean, standard error and the variance with the keys "mean", "std_error" and "variance", respectively.

```
[ ]: num_samples = 10000
burn_in = 100
steps = 100

piquil_stats2 = piquil.statistics(nn_state, num_samples, burn_in=burn_in, steps=steps)
print(
    "Mean PIQuIL: %.4f" % piquil_stats2["mean"], "+/- %.4f" % piquil_stats2["std_error
    '']
)
print("Variance: %.4f" % piquil_stats2["variance"])
```

6.2.2 TFIM Energy

Some observables cannot be computed directly from samples, but instead depend on the RBM as previously mentioned. For example, the magnetization of the TFIM simply depends on the samples the user gives as input. Whereas the TFIM energy is much more complicated. An example for the computation of the energy is provided in the python file *quantum_ising_chain.py*, which takes advantage of qucumber's *Observable* module.

quantum_ising_chain.py comprises of a class that computes the energy of a TFIM (*TFIMChainEnergy*) that inherits properties from the *Observable* module. To instantiate a *TFIMChainEnergy* object, the $\frac{h}{J}$ value must be specified. The trained RBM parameters are from the first tutorial, where the example data was from the TFIM with 10 sites at its critical point ($\frac{h}{J} = 1$).

[]: h = 1

```
tfim_energy = TFIMChainEnergy(h)
```

To go ahead and calculate the mean energy and its standard error from the previously generated samples from this tutorial (new_samples), the *statistics_from_samples* function in the *Observable* module is called upon.

```
[]: energy_stats = tfim_energy.statistics_from_samples(nn_state, new_samples)
print("Mean: %.4f" % energy_stats["mean"], "+/- %.4f" % energy_stats["std_error"])
print("Variance: %.4f" % energy_stats["variance"])
```

The exact value for the energy is -1.2381.

To illustrate how quickly the energy converges as a function of the sampling step (i.e. the number of Gibbs steps to perform to generate a new batch of samples), *steps*, the *Convergence* function in *quantum_ising_chain.py* will do the trick. *Convergence* creates a batch of random samples initially, which is then used to generate a new batch of samples from the RBM. The TFIM energy will be calculated at every Gibbs step. Please note that the samples generated previously (new_samples) are not used here; different samples are generated.

```
[ ]: steps = 200
num_samples = 10000
dict_observables = quantum_ising_chain.Convergence(
    nn_state, tfim_energy, num_samples, steps
)
energy = dict_observables["energies"]
err_energy = dict_observables["error"]
step = np.arange(steps + 1)
E0 = -1.2381
ax = plt.axes()
ax.plot(step, abs((energy - E0) / E0) * 100, color="red")
ax.set_xlim(0, steps)
ax.set_ylim(0, 0.6)
ax.set_ylim(0, 0.6)
ax.set_ylabel("% Error in Energy")
```

One can see a brief transient period in the magnetization observable, before the state of the machine "warms up" to equilibrium. After that, the values fluctuate around the calculated mean.

6.2.3 Adding observables

One may also add / subtract observables with the new observable also retaining the same properties in the *Observables* module. For instance, a new observable can be defined by adding the TFIM energy observable multiplied by an arbitrary constant to the PIQuIL observable.

```
[ ]: new_obs = 0.01 * tfim_energy + piquil
```

The same statistics of this new observable can also be calculated.

```
[ ]: new_obs_stats = new_obs.statistics_from_samples(nn_state, new_samples)
print("Mean: %.4f" % new_obs_stats["mean"], "+/- %.4f" % new_obs_stats["std_error"])
print("Variance: %.4f" % new_obs_stats["variance"])
```

6.2.4 Template for your custom observable

Here is a generic template for you to try using the Observable module yourself.

```
[]: import torch
from qucumber.observables import ObservableBase
class YourObservable(ObservableBase):
    def __init__(self, your_constants):
        super(YourObservable, self).__init__()
        self.your_constants = your_constants
    def apply(self, nn_state, samples):
        # arguments of "apply" must be in this order
        # calculate your observable for each data point
        obs = torch.tensor([42] * len(samples))
        # make sure the observables are on the same device and have the
        # same dtype as the samples
        obs = obs.to(samples)
        # return a torch tensor containing the observable values
        return obs
```

Training while monitoring observables

As seen in the first tutorial that went through reconstructing the wavefunction describing the TFIM with 10 sites at its critical point, the user can evaluate the training in real time with the *MetricEvaluator* and custom functions. What is most likely more impactful in many cases is to calculate an observable, like the energy, during the training process. This is slightly more computationally involved than using the *MetricEvaluator* to evaluate functions because observables require that samples be drawn from the RBM.

Luckily, qucumber also has a module very similar to the *MetricEvaluator*, but for observables. This is called the *ObservableEvaluator*. The following implements the *ObservableEvaluator* to calculate the energy during the training on the TFIM data in the first tutorial. We will use the same hyperparameters as before.

It is assumed that the user has worked through tutorial 3 beforehand. Recall that *quantum_ising_chain.py* contains the *TFIMChainEnergy* class that inherits from the *Observable* module. The exact ground-state energy is -1.2381.

```
import numpy as np
import matplotlib.pyplot as plt
from qucumber.nn_states import PositiveWaveFunction
from qucumber.callbacks import ObservableEvaluator
import qucumber.utils.data as data
from quantum_ising_chain import TFIMChainEnergy
[]: train_data = data.load_data(
        os.path.join("...", "Tutorial1_TrainPosRealWaveFunction", "tfimld_data.txt")
)[0]
nv = train_data.shape[-1]
nh = nv
nn_state = PositiveWaveFunction(num_visible=nv, num_hidden=nh)
```

[]: import os.path

(continues on next page)

(continued from previous page)

```
epochs = 1000
pbs = 100  # pos_batch_size
nbs = 200  # neg_batch_size
lr = 0.01
k = 10
log_every = 100
h = 1
num_samples = 10000
burn_in = 100
steps = 100
tfim_energy = TFIMChainEnergy(h)
```

Now, the ObservableEvaluator can be called. The ObservableEvaluator requires the following arguments.

- 1. **log_every**: the frequency of the training evaluators being calculated is controlled by the *log_every* argument (e.g. *log_every* = 200 means that the *MetricEvaluator* will update the user every 200 epochs)
- 2. A list of *Observable* objects you would like to reference to evaluate the training (arguments required for generating samples to calculate the observables are keyword arguments placed after the list)

The following additional arguments are needed to calculate the statistics on the generated samples during training (these are the arguments of the *statistics* function in the *Observable* module, minus the *nn_state* argument; this gets passed in as an argument to *fit*).

- num_samples: the number of samples to generate internally
- **num_chains**: the number of Markov chains to run in parallel (default = 0)
- **burn_in**: the number of Gibbs steps to perform before recording any samples (default = 1000)
- **steps**: the number of Gibbs steps to perform between each sample (default = 1)

The training evaluators can be printed out via the *verbose=True* statement.

```
[]: callbacks = [
        ObservableEvaluator(
            log_every,
             [tfim_energy],
             verbose=True,
            num_samples=num_samples,
             burn_in=burn_in,
             steps=steps,
         )
    ]
    nn_state.fit(
        train data,
        epochs=epochs,
        pos_batch_size=pbs,
        neg_batch_size=nbs,
        lr=lr,
        k=k,
         callbacks=callbacks,
    )
```

The *callbacks* list returns a list of dictionaries. The mean, standard error and the variance at each epoch can be accessed as follows.

A plot of the energy as a function of the training cycle is presented below.

```
[]: epoch = np.arange(log_every, epochs + 1, log_every)
E0 = -1.2381
ax = plt.axes()
ax.plot(epoch, energies, color="red")
ax.set_xlim(log_every, epochs)
ax.axhline(E0, color="black")
ax.fill_between(epoch, energies - errors, energies + errors, alpha=0.2, color="black")
ax.set_xlabel("Epoch")
ax.set_ylabel("Energy")
ax.grid()
```

RBM

class qucumber.rbm.**BinaryRBM**(*num_visible*, *num_hidden*, *zero_weights=False*, *gpu=True*) Bases: torch.nn.modules.module.Module

effective_energy(v)

The effective energies of the given visible states.

$$\mathcal{E}(v) = -\sum_{j} b_{j} v_{j} - \sum_{i} \log \left[1 + \exp\left(c_{i} + \sum_{j} W_{ij} v_{j}\right) \right]$$

Parameters v (*torch*. *Tensor*) – The visible states.

Returns The effective energies of the given visible states.

Return type torch.Tensor

effective_energy_gradient(v)

The gradients of the effective energies for the given visible states.

Parameters v (torch. Tensor) – The visible states.

Returns 1d vector containing the gradients for all parameters (computed on the given visible states v).

Return type torch.Tensor

gibbs_steps (k, initial_state, overwrite=False)

Performs k steps of Block Gibbs sampling. One step consists of sampling the hidden state h from the conditional distribution p(h | v), and sampling the visible state v from the conditional distribution p(v | h).

Parameters

- **k** (*int*) Number of Block Gibbs steps.
- initial_state (torch.Tensor) The initial state of the Markov Chain. If given, num_samples will be ignored.
- **overwrite** (bool) Whether to overwrite the initial_state tensor, if it is provided.

```
initialize_parameters (zero_weights=False)
Randomize the parameters of the RBM
```

partition (space)

Compute the partition function of the RBM.

Parameters space (torch.Tensor) – A rank 2 tensor of the visible space.

Returns The value of the partition function evaluated at the current state of the RBM.

Return type torch.Tensor

prob_h_given_v(v, out=None)

Given a visible unit configuration, compute the probability vector of the hidden units being on.

Parameters

- h (torch. Tensor) The hidden unit.
- out (torch. Tensor) The output tensor to write to.

Returns The probability of hidden units being active given the visible state.

Return type torch.Tensor

prob_v_given_h(h, out=None)

Given a hidden unit configuration, compute the probability vector of the visible units being on.

Parameters

- h (torch. Tensor) The hidden unit
- **out** (*torch*. *Tensor*) The output tensor to write to.

Returns The probability of visible units being active given the hidden state.

Return type torch.Tensor

sample_h_given_v(v, out=None)

Sample/generate a hidden state given a visible state.

Parameters

- h (torch. Tensor) The visible state.
- **out** (*torch*. *Tensor*) The output tensor to write to.

Returns Tuple containing prob_h_given_v(v) and the sampled hidden state.

Return type tuple(torch.Tensor, torch.Tensor)

sample_v_given_h(h, out=None)

Sample/generate a visible state given a hidden state.

Parameters

- h (torch. Tensor) The hidden state.
- **out** (*torch*. *Tensor*) The output tensor to write to.

Returns Tuple containing prob_v_given_h(h) and the sampled visible state.

Return type tuple(torch.Tensor, torch.Tensor)

Quantum States

9.1 Positive WaveFunction

Bases: qucumber.nn_states.WaveFunctionBase

Class capable of learning WaveFunctionBases with no phase.

Parameters

- **num_visible** (*int*) The number of visible units, ie. the size of the system being learned.
- num_hidden (*int*) The number of hidden units in the internal RBM. Defaults to the number of visible units.
- **gpu** (bool) Whether to perform computations on the default gpu.

amplitude (v)

Compute the (unnormalized) amplitude of a given vector/matrix of visible states.

amplitude
$$(\sigma) = |\psi_{\lambda}(\sigma)| = e^{-\mathcal{E}_{\lambda}(\sigma)/2}$$

Parameters \mathbf{v} (torch. Tensor) – visible states σ

Returns Matrix/vector containing the amplitudes of v

Return type torch.Tensor

static autoload(location, gpu=False)

Initializes a WaveFunctionBase from the parameters in the given location.

Parameters

- **location** (*str or file*) The location to load the model parameters from.
- gpu (bool) Whether the returned model should be on the GPU.

Returns A new WaveFunctionBase initialized from the given parameters. The returned Wave-FunctionBase will be of whichever type this function was called on.

compute_batch_gradients(k, samples_batch, neg_batch)

Compute the gradients of a batch of the training data (*samples_batch*).

Parameters

- k (int) Number of contrastive divergence steps in training.
- **samples_batch** (*torch.Tensor*) Batch of the input samples.
- **neg_batch** (*torch.Tensor*) Batch of the input samples for computing the negative phase.

Returns List containing the gradients of the parameters.

Return type list

compute_normalization(space)

Compute the normalization constant of the wavefunction.

$$Z_{\lambda} = \sqrt{\sum_{\sigma} |\psi_{\lambda}|^2} = \sqrt{\sum_{\sigma} p_{\lambda}(\sigma)}$$

Parameters space (*torch*. *Tensor*) – A rank 2 tensor of the entire visible space.

device

The device that the model is on.

fit (data, epochs=100, pos_batch_size=100, neg_batch_size=None, k=1, lr=0.001, progbar=False, starting_epoch=1, time=False, callbacks=None, optimizer=<class 'torch.optim.sgd.SGD'>, **kwargs)

Train the WaveFunctionBase.

Parameters

- data (np.array) The training samples
- **epochs** (*int*) The number of full training passes through the dataset. Technically, this specifies the index of the *last* training epoch, which is relevant if *starting_epoch* is being set.
- **pos_batch_size** (*int*) The size of batches for the positive phase taken from the data.
- **neg_batch_size** (*int*) The size of batches for the negative phase taken from the data. Defaults to *pos_batch_size*.
- **k** (*int*) The number of contrastive divergence steps.
- lr (float) Learning rate
- **progbar** (*bool or str*) Whether or not to display a progress bar. If "notebook" is passed, will use a Jupyter notebook compatible progress bar.
- **starting_epoch** (*int*) The epoch to start from. Useful if continuing training from a previous state.
- **callbacks** (*list* [qucumber.callbacks.Callback]) Callbacks to run while training.
- **optimizer** (torch.optim.Optimizer) The constructor of a torch optimizer.
- kwargs Keyword arguments to pass to the optimizer
```
generate_hilbert_space (size=None, device=None)
Generates Hilbert space of dimension 2<sup>size</sup>.
```

Parameters

- **size** (*int*) The size of each element of the Hilbert space. Defaults to the number of visible units.
- **device** The device to create the Hilbert space matrix on. Defaults to the device this model is on.

Returns A tensor with all the basis states of the Hilbert space.

Return type torch.Tensor

gradient(v)

Compute the gradient of the effective energy for a batch of states.

 $\nabla_{\lambda} \mathcal{E}_{\lambda}(\sigma)$

Parameters \mathbf{v} (torch.Tensor) – visible states σ

Returns A single tensor containing all of the parameter gradients.

Return type torch.Tensor

load (location)

Loads the WaveFunctionBase parameters from the given location ignoring any metadata stored in the file. Overwrites the WaveFunctionBase's parameters.

Note: The WaveFunctionBase object on which this function is called must have the same parameter shapes as the one who's parameters are being loaded.

Parameters location (*str or file*) – The location to load the WaveFunctionBase parameters from.

max_size

Maximum size of the Hilbert space for full enumeration

networks

A list of the names of the internal RBMs.

phase(v)

Compute the phase of a given vector/matrix of visible states.

In the case of a Positive WaveFunctionBase, the phase is just zero.

Parameters \mathbf{v} (torch.Tensor) – visible states σ

Returns Matrix/vector containing the phases of v

Return type torch.Tensor

probability (v, Z)

Evaluates the probability of the given vector(s) of visible states.

Parameters

- **v** (torch. Tensor) The visible states.
- **Z** (*float*) The partition function.

Returns The probability of the given vector(s) of visible units.

Return type torch.Tensor

psi(v)

Compute the (unnormalized) wavefunction of a given vector/matrix of visible states.

$$\psi_{\lambda}(\sigma) = e^{-\mathcal{E}_{\lambda}(\sigma)/2}$$

Parameters \mathbf{v} (torch. Tensor) – visible states σ

Returns Complex object containing the value of the wavefunction for each visible state

Return type torch.Tensor

rbm_am

The RBM to be used to learn the wavefunction amplitude.

reinitialize_parameters()

Randomize the parameters of the internal RBMs.

sample (k, num_samples=1, initial_state=None, overwrite=False)

Performs k steps of Block Gibbs sampling. One step consists of sampling the hidden state h from the conditional distribution $p_{\lambda}(h|v)$, and sampling the visible state v from the conditional distribution $p_{\lambda}(v|h)$.

Parameters

- k (int) Number of Block Gibbs steps.
- num_samples (*int*) The number of samples to generate.
- initial_state (torch.Tensor) The initial state of the Markov Chain. If given, num_samples will be ignored.
- **overwrite** (bool) Whether to overwrite the initial_state tensor, if it is provided.

save (location, metadata=None)

Saves the WaveFunctionBase parameters to the given location along with any given metadata.

Parameters

- location (str or file) The location to save the data.
- **metadata** (*dict*) Any extra metadata to store alongside the WaveFunctionBase parameters.

stop_training

If True, will not train.

If this property is set to *True* during the training cycle, training will terminate once the current batch or epoch ends (depending on when *stop_training* was set).

subspace_vector (num, size=None, device=None)

Generates a single vector from the Hilbert space of dimension 2^{size} .

Parameters

- **size** (*int*) The size of each element of the Hilbert space.
- **num** (*int*) The specific vector to return from the Hilbert space. Since the Hilbert space can be represented by the set of binary strings of length *size*, *num* is equivalent to the decimal representation of the returned vector.
- device The device to create the vector on. Defaults to the device this model is on.

Returns A state from the Hilbert space.

Return type torch.Tensor

9.2 Complex WaveFunction

class qucumber.nn_states.ComplexWaveFunction(num_visible, num_hidden=None, unitary_dict=None, gpu=True)

 $Bases: \verb"qucumber.nn_states.WaveFunctionBase"$

Class capable of learning WaveFunctionBases with a non-zero phase.

Parameters

- **num_visible** (*int*) The number of visible units, ie. the size of the system being learned.
- num_hidden (*int*) The number of hidden units in both internal RBMs. Defaults to the number of visible units.
- **unitary_dict** (*dict[str, torch.Tensor]*) A dictionary mapping unitary names to their matrix representations.
- **gpu** (bool) Whether to perform computations on the default gpu.

amplitude (v)

Compute the (unnormalized) amplitude of a given vector/matrix of visible states.

amplitude(
$$\sigma$$
) = $|\psi_{\lambda\mu}(\sigma)| = e^{-\mathcal{E}_{\lambda}(\sigma)/2}$

Parameters \mathbf{v} (torch. Tensor) – visible states σ .

Returns Vector containing the amplitudes of the given states.

Return type torch.Tensor

static autoload(location, gpu=False)

Initializes a WaveFunctionBase from the parameters in the given location.

Parameters

- location (*str or file*) The location to load the model parameters from.
- **gpu** (bool) Whether the returned model should be on the GPU.
- **Returns** A new WaveFunctionBase initialized from the given parameters. The returned Wave-FunctionBase will be of whichever type this function was called on.

compute_batch_gradients (k, samples_batch, neg_batch, bases_batch=None)

Compute the gradients of a batch of the training data (*samples_batch*).

If measurements are taken in bases other than the reference basis, a list of bases (*bases_batch*) must also be provided.

Parameters

- k (int) Number of contrastive divergence steps in training.
- samples_batch (torch.Tensor) Batch of the input samples.
- **neg_batch** (*torch.Tensor*) Batch of the input samples for computing the negative phase.
- **bases_batch** (*np.array*) Batch of the input bases corresponding to the samples in *samples_batch*.

Returns List containing the gradients of the parameters.

Return type list

compute_normalization(space)

Compute the normalization constant of the wavefunction.

$$Z_{\lambda} = \sqrt{\sum_{\sigma} |\psi_{\lambda\mu}|^2} = \sqrt{\sum_{\sigma} p_{\lambda}(\sigma)}$$

Parameters space (*torch*. *Tensor*) – A rank 2 tensor of the entire visible space.

device

The device that the model is on.

fit (data, epochs=100, pos_batch_size=100, neg_batch_size=None, k=1, lr=0.001, input_bases=None, progbar=False, starting_epoch=1, time=False, callbacks=None, optimizer=<class 'torch.optim.sgd.SGD'>, **kwargs) Train the WaveFunctionBase.

Parameters

- data (np.array) The training samples
- **epochs** (*int*) The number of full training passes through the dataset. Technically, this specifies the index of the *last* training epoch, which is relevant if *starting_epoch* is being set.
- **pos_batch_size** (*int*) The size of batches for the positive phase taken from the data.
- **neg_batch_size** (*int*) The size of batches for the negative phase taken from the data. Defaults to *pos_batch_size*.
- **k** (*int*) The number of contrastive divergence steps.
- **lr** (*float*) Learning rate
- **input_bases** (*np.array*) The measurement bases for each sample. Must be provided if training a ComplexWaveFunction.
- **progbar** (*bool or str*) Whether or not to display a progress bar. If "notebook" is passed, will use a Jupyter notebook compatible progress bar.
- **starting_epoch** (*int*) The epoch to start from. Useful if continuing training from a previous state.
- **callbacks** (*list* [qucumber.callbacks.CallbackBase]) Callbacks to run while training.
- **optimizer** (torch.optim.Optimizer) The constructor of a torch optimizer.
- kwargs Keyword arguments to pass to the optimizer

generate_hilbert_space (size=None, device=None)

Generates Hilbert space of dimension 2^{size} .

Parameters

- **size** (*int*) The size of each element of the Hilbert space. Defaults to the number of visible units.
- device The device to create the Hilbert space matrix on. Defaults to the device this model is on.

Returns A tensor with all the basis states of the Hilbert space.

Return type torch.Tensor

gradient (basis, sample)

Compute the gradient of a sample, measured in different bases.

Parameters

- **basis** (*np.array*) A set of bases.
- **sample** (*np.array*) A sample to compute the gradient of.

Returns A list of 2 tensors containing the parameters of each of the internal RBMs.

Return type list[torch.Tensor]

load(location)

Loads the WaveFunctionBase parameters from the given location ignoring any metadata stored in the file. Overwrites the WaveFunctionBase's parameters.

Note: The WaveFunctionBase object on which this function is called must have the same parameter shapes as the one who's parameters are being loaded.

Parameters location (*str or file*) – The location to load the WaveFunctionBase parameters from.

max_size

Maximum size of the Hilbert space for full enumeration

networks

A list of the names of the internal RBMs.

phase(v)

Compute the phase of a given vector/matrix of visible states.

phase(σ) = $-\mathcal{E}_{\mu}(\sigma)/2$

Parameters \mathbf{v} (torch. Tensor) – visible states σ .

Returns Vector containing the phases of the given states.

Return type torch.Tensor

probability (v, Z)

Evaluates the probability of the given vector(s) of visible states.

Parameters

- **v** (torch. Tensor) The visible states.
- **Z** (*float*) The partition function.

Returns The probability of the given vector(s) of visible units.

Return type torch.Tensor

psi(v)

Compute the (unnormalized) wavefunction of a given vector/matrix of visible states.

$$\psi_{\lambda\mu}(\sigma) = e^{-[\mathcal{E}_{\lambda}(\sigma) + i\mathcal{E}_{\mu}(\sigma)]/2}$$

Parameters \mathbf{v} (torch. Tensor) – visible states σ

Returns Complex object containing the value of the wavefunction for each visible state

Return type torch.Tensor

rbm_am

The RBM to be used to learn the wavefunction amplitude.

rbm_ph

RBM used to learn the wavefunction phase.

```
reinitialize_parameters()
```

Randomize the parameters of the internal RBMs.

sample (k, num_samples=1, initial_state=None, overwrite=False)

Performs k steps of Block Gibbs sampling. One step consists of sampling the hidden state h from the conditional distribution $p_{\lambda}(h|v)$, and sampling the visible state v from the conditional distribution $p_{\lambda}(v|h)$.

Parameters

- k (int) Number of Block Gibbs steps.
- num_samples (*int*) The number of samples to generate.
- initial_state (torch.Tensor) The initial state of the Markov Chain. If given, num_samples will be ignored.
- **overwrite** (*bool*) Whether to overwrite the initial_state tensor, if it is provided.

save (location, metadata=None)

Saves the WaveFunctionBase parameters to the given location along with any given metadata.

Parameters

- location (str or file) The location to save the data.
- **metadata** (*dict*) Any extra metadata to store alongside the WaveFunctionBase parameters.

stop_training

If True, will not train.

If this property is set to *True* during the training cycle, training will terminate once the current batch or epoch ends (depending on when *stop_training* was set).

subspace_vector (num, size=None, device=None)

Generates a single vector from the Hilbert space of dimension 2^{size}.

Parameters

- **size** (*int*) The size of each element of the Hilbert space.
- **num** (*int*) The specific vector to return from the Hilbert space. Since the Hilbert space can be represented by the set of binary strings of length *size*, *num* is equivalent to the decimal representation of the returned vector.
- device The device to create the vector on. Defaults to the device this model is on.

Returns A state from the Hilbert space.

Return type torch.Tensor

9.3 Abstract WaveFunction

Note: This is an Abstract Base Class, it is not meant to be used directly. The following API reference is mostly for developers.

class qucumber.nn_states.WaveFunctionBase

Bases: abc.ABC

Abstract Base Class for WaveFunctionBases.

amplitude (v)

Compute the (unnormalized) amplitude of a given vector/matrix of visible states.

amplitude(σ) = $|\psi(\sigma)|$

Parameters \mathbf{v} (torch.Tensor) – visible states σ

Returns Matrix/vector containing the amplitudes of v

Return type torch.Tensor

```
static autoload(location, gpu=False)
```

Initializes a WaveFunctionBase from the parameters in the given location.

Parameters

- location (*str or file*) The location to load the model parameters from.
- **gpu** (bool) Whether the returned model should be on the GPU.

Returns A new WaveFunctionBase initialized from the given parameters. The returned Wave-FunctionBase will be of whichever type this function was called on.

compute_batch_gradients (*k*, *samples_batch*, *neg_batch*, *bases_batch=None*) Compute the gradients of a batch of the training data (*samples_batch*).

If measurements are taken in bases other than the reference basis, a list of bases (*bases_batch*) must also be provided.

Parameters

- **k** (*int*) Number of contrastive divergence steps in training.
- **samples_batch** (*torch*. *Tensor*) Batch of the input samples.
- **neg_batch** (*torch.Tensor*) Batch of the input samples for computing the negative phase.
- **bases_batch** (*np.array*) Batch of the input bases corresponding to the samples in *samples_batch*.

Returns List containing the gradients of the parameters.

Return type list

compute_normalization(space)

Compute the normalization constant of the wavefunction.

$$Z_{\lambda} = \sqrt{\sum_{\sigma} |\psi_{\lambda\mu}|^2} = \sqrt{\sum_{\sigma} p_{\lambda}(\sigma)}$$

Parameters space (torch. Tensor) – A rank 2 tensor of the entire visible space.

device

The device that the model is on.

fit (data, epochs=100, pos_batch_size=100, neg_batch_size=None, k=1, lr=0.001, input_bases=None, progbar=False, starting_epoch=1, time=False, callbacks=None, optimizer=<class 'torch.optim.sgd.SGD'>, **kwargs) Train the WaveFunctionBase.

Parameters

- data (np.array) The training samples
- **epochs** (*int*) The number of full training passes through the dataset. Technically, this specifies the index of the *last* training epoch, which is relevant if *starting_epoch* is being set.
- **pos_batch_size** (*int*) The size of batches for the positive phase taken from the data.
- **neg_batch_size** (*int*) The size of batches for the negative phase taken from the data. Defaults to *pos_batch_size*.
- **k** (*int*) The number of contrastive divergence steps.
- **lr** (*float*) Learning rate
- **input_bases** (*np.array*) The measurement bases for each sample. Must be provided if training a ComplexWaveFunction.
- **progbar** (*bool or str*) Whether or not to display a progress bar. If "notebook" is passed, will use a Jupyter notebook compatible progress bar.
- **starting_epoch** (*int*) The epoch to start from. Useful if continuing training from a previous state.
- **callbacks** (*list* [qucumber.callbacks.CallbackBase]) Callbacks to run while training.
- **optimizer** (torch.optim.Optimizer) The constructor of a torch optimizer.
- **kwargs** Keyword arguments to pass to the optimizer

generate_hilbert_space(size=None, device=None)

Generates Hilbert space of dimension 2^{size} .

Parameters

- **size** (*int*) The size of each element of the Hilbert space. Defaults to the number of visible units.
- **device** The device to create the Hilbert space matrix on. Defaults to the device this model is on.

Returns A tensor with all the basis states of the Hilbert space.

Return type torch.Tensor

gradient()

Compute the gradient of a set of samples.

load(location)

Loads the WaveFunctionBase parameters from the given location ignoring any metadata stored in the file. Overwrites the WaveFunctionBase's parameters.

Note: The WaveFunctionBase object on which this function is called must have the same parameter shapes as the one who's parameters are being loaded.

Parameters location (*str or file*) – The location to load the WaveFunctionBase parameters from.

max_size

Maximum size of the Hilbert space for full enumeration

networks

A list of the names of the internal RBMs.

phase(v)

Compute the phase of a given vector/matrix of visible states.

phase(σ)

Parameters \mathbf{v} (torch.Tensor) – visible states σ

Returns Matrix/vector containing the phases of v

Return type torch.Tensor

probability (v, Z)

Evaluates the probability of the given vector(s) of visible states.

Parameters

- **v** (torch. Tensor) The visible states.
- **Z** (*float*) The partition function.

Returns The probability of the given vector(s) of visible units.

Return type torch.Tensor

psi(v)

Compute the (unnormalized) wavefunction of a given vector/matrix of visible states.

 $\psi(\sigma)$

Parameters \mathbf{v} (torch. Tensor) – visible states σ

Returns Complex object containing the value of the wavefunction for each visible state

Return type torch.Tensor

rbm_am

The RBM to be used to learn the wavefunction amplitude.

reinitialize_parameters()

Randomize the parameters of the internal RBMs.

sample (k, num_samples=1, initial_state=None, overwrite=False)

Performs k steps of Block Gibbs sampling. One step consists of sampling the hidden state h from the conditional distribution $p_{\lambda}(h|v)$, and sampling the visible state v from the conditional distribution $p_{\lambda}(v|h)$.

- k (int) Number of Block Gibbs steps.
- num_samples (*int*) The number of samples to generate.
- initial_state (torch.Tensor) The initial state of the Markov Chain. If given, num_samples will be ignored.
- **overwrite** (bool) Whether to overwrite the initial_state tensor, if it is provided.

save (location, metadata=None)

Saves the WaveFunctionBase parameters to the given location along with any given metadata.

Parameters

- **location** (*str or file*) The location to save the data.
- **metadata** (*dict*) Any extra metadata to store alongside the WaveFunctionBase parameters.

stop_training

If True, will not train.

If this property is set to *True* during the training cycle, training will terminate once the current batch or epoch ends (depending on when *stop_training* was set).

subspace_vector (num, size=None, device=None)

Generates a single vector from the Hilbert space of dimension 2^{size} .

Parameters

- **size** (*int*) The size of each element of the Hilbert space.
- **num** (*int*) The specific vector to return from the Hilbert space. Since the Hilbert space can be represented by the set of binary strings of length *size*, *num* is equivalent to the decimal representation of the returned vector.
- device The device to create the vector on. Defaults to the device this model is on.

Returns A state from the Hilbert space.

Return type torch.Tensor

CHAPTER 10

Callbacks

class qucumber.callbacks.**CallbackBase** Base class for callbacks.

on_batch_end (*nn_state*, *epoch*, *batch*) Called at the end of each batch.

Parameters

- nn_state (WaveFunction) The WaveFunction being trained.
- **epoch** (*int*) The current epoch.
- **batch** (*int*) The current batch index.

on_batch_start (*nn_state*, *epoch*, *batch*) Called at the start of each batch.

alled at the start of each bate

Parameters

- nn_state (WaveFunction) The WaveFunction being trained.
- **epoch** (*int*) The current epoch.
- **batch** (*int*) The current batch index.
- on_epoch_end(nn_state, epoch)

Called at the end of each epoch.

Parameters

- nn_state (WaveFunction) The WaveFunction being trained.
- **epoch** (*int*) The current epoch.
- on_epoch_start (nn_state, epoch)

Called at the start of each epoch.

Parameters

• **nn_state** (*WaveFunction*) – The WaveFunction being trained.

• epoch (*int*) – The current epoch.

on_train_end(nn_state)

Called at the end of the training cycle.

Parameters nn_state (WaveFunction) - The WaveFunction being trained.

```
on_train_start (nn_state)
```

Called at the start of the training cycle.

Parameters nn_state (WaveFunction) – The WaveFunction being trained.

class	qucumber.	.callbacks	LambdaCallback (on_train_start=None,	on_train_end=None,		
			on_epoch_start=None,	on_epoch_end=None,		
			on_batch_start=None, on_	one, on_batch_end=None)		

Class for creating simple callbacks.

This callback is constructed using the passed functions that will be called at the appropriate time.

Parameters

- on_train_start (callable or None) A function to be called at the start of the training cycle. Must follow the same signature as CallbackBase.on_train_start.
- on_train_end(callable or None) A function to be called at the end of the training cycle. Must follow the same signature as CallbackBase.on_train_end.
- on_epoch_start (callable or None) A function to be called at the start of every epoch. Must follow the same signature as CallbackBase.on_epoch_start.
- **on_epoch_end** (*callable or None*) A function to be called at the end of every epoch. Must follow the same signature as *CallbackBase.on_epoch_end*.
- **on_batch_start** (*callable or None*) A function to be called at the start of every batch. Must follow the same signature as *CallbackBase.on_batch_start*.
- on_batch_end (callable or None) A function to be called at the end of every batch. Must follow the same signature as CallbackBase.on_batch_end.
- **class** qucumber.callbacks.**ModelSaver** (*period*, *folder_path*, *file_name*, *save_initial=True*, *meta-data=None*, *metadata* only=False)

CallbackBase which allows model parameters (along with some metadata) to be saved to disk at regular intervals.

This CallbackBase is called at the end of each epoch. If *save_initial* is *True*, will also be called at the start of the training cycle.

- **period** (*int*) Frequency of model saving (in epochs).
- **folder_path** (*str*) The directory in which to save the files
- **file_name** (*str*) The name of the output files. Should be a format string with one blank, which will be filled with either the epoch number or the word "initial".
- **save_initial** (bool) Whether to save the initial parameters (and metadata).
- **metadata** (*callable or dict or None*) The metadata to save to disk with the model parameters Can be either a function or a dictionary. In the case of a function, it must take 2 arguments the RBM being trained, and the current epoch number, and then return a dictionary containing the metadata to be saved.
- **metadata_only** (bool) Whether to save only the metadata to disk.

CallbackBase which logs output at regular intervals.

This CallbackBase is called at the end of each epoch.

Parameters

- **period** (*int*) Logging frequency (in epochs).
- **logger_fn** (*callable*) The function used for logging. Must take 1 string as an argument. Defaults to the standard *print* function.
- msg_gen (callable) A callable which generates the string to be logged. Must take 2 positional arguments: the RBM being trained and the current epoch. It must also be able to take some keyword arguments.
- ****kwargs** Keyword arguments which will be passed to *msg_gen*.

Stop training once the model stops improving. The specific criterion for stopping is:

$$\left|\frac{M_{t-p} - M_t}{M_{t-p}}\right| < \epsilon$$

where M_t is the metric value at the current evaluation (time t), p is the "patience" parameter, and ϵ is the tolerance.

This CallbackBase is called at the end of each epoch.

Parameters

- **period** (*int*) Frequency with which the callback checks whether training has converged (in epochs).
- **tolerance** (*float*) The maximum relative change required to consider training as having converged.
- **patience** (*int*) How many intervals to wait before claiming the training has converged.
- **evaluator_callback** (*MetricEvaluator* or *ObservableEvaluator*) An instance of *MetricEvaluator* or *ObservableEvaluator* which computes the metric that we want to check for convergence.
- **quantity_name** (*str*) The name of the metric/observable stored in *evalua-tor_callback*.

class qucumber.callbacks.VarianceBasedEarlyStopping(period, tolerance, patience, evaluator_callback, quantity_name,

variance_name)

Stop training once the model stops improving. This is a variation on the *EarlyStopping* class which takes the variance of the metric into account. The specific criterion for stopping is:

$$\left|\frac{M_{t-p} - M_t}{\sigma_{t-p}}\right| < \kappa$$

where M_t is the metric value at the current evaluation (time t), p is the "patience" parameter, σ_t is the variance of the metric, and κ is the tolerance.

This CallbackBase is called at the end of each epoch.

- **period** (*int*) Frequency with which the callback checks whether training has converged (in epochs).
- **tolerance** (*float*) The maximum (standardized) change required to consider training as having converged.
- **patience** (*int*) How many intervals to wait before claiming the training has converged.
- **evaluator_callback** (*MetricEvaluator* or *ObservableEvaluator*) An instance of *MetricEvaluator* or *ObservableEvaluator* which computes the metric/observable that we want to check for convergence.
- quantity_name (*str*) The name of the metric/obserable stored in *evaluator_callback*.
- **variance_name** (*str*) The name of the variance stored in *evaluator_callback*.

Evaluate and hold on to the results of the given metric(s).

This CallbackBase is called at the end of each epoch.

Note: Since CallbackBases are given to fit as a list, they will be called in a deterministic order. It is therefore recommended that instances of *MetricEvaluator* be among the first callbacks in the list passed to fit, as one would often use it in conjunction with other callbacks like *EarlyStopping* which may depend on *MetricEvaluator* having been called.

Parameters

- **period** (*int*) Frequency with which the callback evaluates the given metric(s).
- **metrics** (*dict* (*str*, *callable*)) A dictionary of callables where the keys are the names of the metrics and the callables take the WaveFunction being trained as their positional argument, along with some keyword arguments. The metrics are evaluated and put into an internal dictionary structure resembling the structure of *metrics*.
- **verbose** (*bool*) Whether to print metrics to stdout.
- log(str) A filepath to log metric values to in CSV format.
- ****metric_kwargs** Keyword arguments to be passed to *metrics*.

_getattr__(*metric*)

Return an array of all recorded values of the given metric.

Parameters metric (*str*) – The metric to retrieve.

Returns The past values of the metric.

Return type np.array

len()

Return the number of timesteps that metrics have been evaluated for.

Return type int

clear_history()

Delete all metric values the instance is currently storing.

epochs

Return a list of all epochs that have been recorded.

Return type np.array

get_value (name, index=None)

Retrieve the value of the desired metric from the given timestep.

Parameters

- **name** (*str*) The name of the metric to retrieve.
- **index** (*int* or *None*) The index/timestep from which to retrieve the metric. Negative indices are supported. If None, will just get the most recent value.

names

The names of the tracked metrics.

Return type list[str]

Evaluate and hold on to the results of the given observable(s).

This CallbackBase is called at the end of each epoch.

Note: Since CallbackBases are given to fit as a list, they will be called in a deterministic order. It is therefore recommended that instances of *ObservableEvaluator* be among the first callbacks in the list passed to fit, as one would often use it in conjunction with other callbacks like *EarlyStopping* which may depend on *ObservableEvaluator* having been called.

Parameters

- **period** (*int*) Frequency with which the callback evaluates the given observables(s).
- **observables** (*list* (*qucumber*. *observables*. *Observable*)) A list of Observables. Observable statistics are evaluated by sampling the WaveFunction. Note that observables that have the same name will conflict, and precedence will be given to the right-most observable argument.
- **verbose** (*bool*) Whether to print metrics to stdout.
- log (*str*) A filepath to log metric values to in CSV format.
- ****sampling_kwargs** Keyword arguments to be passed to *Observable.statistics*. Ex. *num_samples, num_chains, burn_in, steps*.

_getattr__(*observable*)

Return an ObservableStatistics containing recorded statistics of the given observable.

Parameters observable (*str*) – The observable to retrieve.

Returns The past values of the observable.

Return type ObservableStatistics

len()

Return the number of timesteps that observables have been evaluated for.

Return type int

clear_history()

Delete all statistics the instance is currently storing.

epochs

Return a list of all epochs that have been recorded.

Return type np.array

get_value (name, index=None)

Retrieve the statistics of the desired observable from the given timestep.

Parameters

- **name** (*str*) The name of the observable to retrieve.
- **index** (*int* or *None*) The index/timestep from which to retrieve the observable. Negative indices are supported. If None, will just get the most recent value.

names

The names of the tracked observables.

Return type list[str]

class qucumber.callbacks.Timer(verbose=True)

CallbackBase which records the training time.

This CallbackBase is always called at the start and end of training. It will run at the end of an epoch or batch if the given model's *stop_training* property is set to True.

Parameters verbose (bool) – Whether to print the elapsed time at the end of training.

CHAPTER 11

Observables

11.1 Pauli Operators

```
class qucumber.observables.SigmaZ
Bases: qucumber.observables.ObservableBase
```

The σ_z observable.

Computes the magnetization in the Z direction of a spin chain.

apply (*nn_state*, *samples*)

Computes the magnetization of each sample given a batch of samples.

Parameters

- **nn_state** (qucumber.nn_states.WaveFunction) The WaveFunction that drew the samples.
- samples (torch.Tensor) A batch of samples to calculate the observable on. Must be using the $\sigma_i = 0, 1$ convention.

name

The name of the ObservableBase.

sample (nn_state, k, num_samples=1, initial_state=None, overwrite=False)
Draws samples of the observable using the given WaveFunction.

- **nn_state** (*qucumber.nn_states.WaveFunction*) The WaveFunction to draw samples from.
- **k** (*int*) The number of Gibbs Steps to perform before drawing a sample.
- **num_samples** (*int*) The number of samples to draw.
- initial_state (torch.Tensor) The initial state of the Markov Chain. If given, num_samples will be ignored.

• **overwrite** (*bool*) – Whether to overwrite the initial_state tensor, if it is provided, with the updated state of the Markov chain.

statistics (nn_state, num_samples, num_chains=0, burn_in=1000, steps=1)

Estimates the expected value, variance, and the standard error of the observable over the distribution defined by the WaveFunction.

Parameters

- nn_state (qucumber.nn_states.WaveFunction) The WaveFunction to draw samples from.
- **num_samples** (*int*) The number of samples to draw. The actual number of samples drawn may be slightly higher if *num_samples % num_chains != 0*.
- **num_chains** (*int*) The number of Markov chains to run in parallel; if 0, will use a number of chains equal to *num_samples*.
- burn_in (int) The number of Gibbs Steps to perform before recording any samples.
- **steps** (*int*) The number of Gibbs Steps to take between each sample.
- **Returns** A dictionary containing the (estimated) expected value (key: "mean"), variance (key: "variance"), and standard error (key: "std_error") of the observable.

Return type dict(str, float)

statistics_from_samples (nn_state, samples)

Estimates the expected value, variance, and the standard error of the observable using the given samples.

Parameters

- **nn_state** (qucumber.nn_states.WaveFunction) The WaveFunction that drew the samples.
- samples (torch. Tensor) A batch of sample states to calculate the observable on.

symbol

The algebraic symbol representing the ObservableBase.

class qucumber.observables.SigmaX

 $Bases: \verb+qucumber.observables.ObservableBase$

The σ_x observable

Computes the magnetization in the X direction of a spin chain.

apply (nn_state, samples)

Computes the magnetization along X of each sample in the given batch of samples.

Parameters

- **nn_state** (qucumber.nn_states.WaveFunction) The WaveFunction that drew the samples.
- samples (torch.Tensor) A batch of samples to calculate the observable on. Must be using the $\sigma_i = 0, 1$ convention.

name

The name of the ObservableBase.

sample (nn_state, k, num_samples=1, initial_state=None, overwrite=False)
Draws samples of the observable using the given WaveFunction.

- **nn_state** (*qucumber.nn_states.WaveFunction*) The WaveFunction to draw samples from.
- **k** (*int*) The number of Gibbs Steps to perform before drawing a sample.
- **num_samples** (*int*) The number of samples to draw.
- initial_state (torch.Tensor) The initial state of the Markov Chain. If given, num_samples will be ignored.
- **overwrite** (*bool*) Whether to overwrite the initial_state tensor, if it is provided, with the updated state of the Markov chain.

statistics (nn_state, num_samples, num_chains=0, burn_in=1000, steps=1)

Estimates the expected value, variance, and the standard error of the observable over the distribution defined by the WaveFunction.

Parameters

- **nn_state** (qucumber.nn_states.WaveFunction) The WaveFunction to draw samples from.
- **num_samples** (*int*) The number of samples to draw. The actual number of samples drawn may be slightly higher if *num_samples* % *num_chains* != 0.
- **num_chains** (*int*) The number of Markov chains to run in parallel; if 0, will use a number of chains equal to *num_samples*.
- **burn_in** (*int*) The number of Gibbs Steps to perform before recording any samples.
- **steps** (*int*) The number of Gibbs Steps to take between each sample.

Returns A dictionary containing the (estimated) expected value (key: "mean"), variance (key: "variance"), and standard error (key: "std_error") of the observable.

Return type dict(str, float)

statistics_from_samples(nn_state, samples)

Estimates the expected value, variance, and the standard error of the observable using the given samples.

Parameters

- **nn_state** (qucumber.nn_states.WaveFunction) The WaveFunction that drew the samples.
- samples (torch.Tensor) A batch of sample states to calculate the observable on.

symbol

The algebraic symbol representing the ObservableBase.

class qucumber.observables.SigmaY

Bases: qucumber.observables.ObservableBase

The σ_y observable

Computes the magnetization in the Y direction of a spin chain.

apply (nn_state, samples)

Computes the magnetization along Y of each sample in the given batch of samples.

Parameters

• **nn_state** (qucumber.nn_states.WaveFunction) - The WaveFunction that drew the samples.

• samples (torch.Tensor) – A batch of samples to calculate the observable on. Must be using the $\sigma_i = 0, 1$ convention.

name

The name of the ObservableBase.

sample (nn_state, k, num_samples=1, initial_state=None, overwrite=False)
Draws samples of the observable using the given WaveFunction.

Parameters

- **nn_state** (*qucumber.nn_states.WaveFunction*) The WaveFunction to draw samples from.
- **k** (*int*) The number of Gibbs Steps to perform before drawing a sample.
- **num_samples** (*int*) The number of samples to draw.
- initial_state (torch.Tensor) The initial state of the Markov Chain. If given, num_samples will be ignored.
- **overwrite** (*bool*) Whether to overwrite the initial_state tensor, if it is provided, with the updated state of the Markov chain.

statistics (nn_state, num_samples, num_chains=0, burn_in=1000, steps=1)

Estimates the expected value, variance, and the standard error of the observable over the distribution defined by the WaveFunction.

Parameters

- **nn_state** (*qucumber.nn_states.WaveFunction*) The WaveFunction to draw samples from.
- **num_samples** (*int*) The number of samples to draw. The actual number of samples drawn may be slightly higher if *num_samples* % *num_chains* != 0.
- **num_chains** (*int*) The number of Markov chains to run in parallel; if 0, will use a number of chains equal to *num_samples*.
- **burn_in** (*int*) The number of Gibbs Steps to perform before recording any samples.
- **steps** (*int*) The number of Gibbs Steps to take between each sample.
- **Returns** A dictionary containing the (estimated) expected value (key: "mean"), variance (key: "variance"), and standard error (key: "std_error") of the observable.

Return type dict(str, float)

statistics_from_samples (nn_state, samples)

Estimates the expected value, variance, and the standard error of the observable using the given samples.

Parameters

- **nn_state** (qucumber.nn_states.WaveFunction) The WaveFunction that drew the samples.
- samples (torch.Tensor) A batch of sample states to calculate the observable on.

symbol

The algebraic symbol representing the ObservableBase.

11.2 Neighbour Interactions

```
class qucumber.observables.NeighbourInteraction(periodic_bcs=False, c=1)
Bases: qucumber.observables.ObservableBase
```

The $\sigma_i^z \sigma_{i+c}^z$ observable

Computes the *c*-th nearest neighbour interaction for a spin chain with either open or periodic boundary conditions.

Parameters

- **periodic_bcs** (bool) Specifies whether the system has periodic boundary conditions.
- **c** (*int*) Interaction distance.

apply (*nn_state*, *samples*)

Computes the energy of this neighbour interaction for each sample given a batch of samples.

Parameters

- **nn_state** (qucumber.nn_states.WaveFunction) The WaveFunction that drew the samples.
- samples (torch.Tensor) A batch of samples to calculate the observable on. Must be using the $\sigma_i = 0, 1$ convention.

name

The name of the ObservableBase.

sample (nn_state, k, num_samples=1, initial_state=None, overwrite=False)
Draws samples of the observable using the given WaveFunction.

Parameters

- **nn_state** (*qucumber.nn_states.WaveFunction*) The WaveFunction to draw samples from.
- **k** (*int*) The number of Gibbs Steps to perform before drawing a sample.
- **num_samples** (*int*) The number of samples to draw.
- initial_state (torch.Tensor) The initial state of the Markov Chain. If given, num_samples will be ignored.
- **overwrite** (*bool*) Whether to overwrite the initial_state tensor, if it is provided, with the updated state of the Markov chain.

statistics (nn_state, num_samples, num_chains=0, burn_in=1000, steps=1)

Estimates the expected value, variance, and the standard error of the observable over the distribution defined by the WaveFunction.

- **nn_state** (*qucumber.nn_states.WaveFunction*) The WaveFunction to draw samples from.
- **num_samples** (*int*) The number of samples to draw. The actual number of samples drawn may be slightly higher if *num_samples* % *num_chains* != 0.
- **num_chains** (*int*) The number of Markov chains to run in parallel; if 0, will use a number of chains equal to *num_samples*.
- **burn_in** (*int*) The number of Gibbs Steps to perform before recording any samples.

- **steps** (*int*) The number of Gibbs Steps to take between each sample.
- **Returns** A dictionary containing the (estimated) expected value (key: "mean"), variance (key: "variance"), and standard error (key: "std_error") of the observable.

Return type dict(str, float)

statistics_from_samples (nn_state, samples)

Estimates the expected value, variance, and the standard error of the observable using the given samples.

Parameters

- **nn_state** (qucumber.nn_states.WaveFunction) The WaveFunction that drew the samples.
- samples (torch. Tensor) A batch of sample states to calculate the observable on.

symbol

The algebraic symbol representing the ObservableBase.

11.3 Abstract Observable

Note: This is an Abstract Base Class, it is not meant to be used directly. The following API reference is mostly for developers.

CHAPTER 12

Complex Algebra

qucumber.utils.cplx.absolute_value(x)

Computes the complex absolute value elementwise.

Parameters x (torch. Tensor) – A complex tensor.

Returns A real tensor.

Return type torch.Tensor

qucumber.utils.cplx.conjugate(x)

A function that takes the conjugate transpose of the argument.

Parameters x (*torch*. *Tensor*) – A complex vector or matrix.

Returns The conjugate of x.

Return type torch.Tensor

qucumber.utils.cplx.elementwise_division(x, y)

Elementwise division of x by y.

Parameters

- **x** (torch. Tensor) A complex tensor.
- **y** (torch.Tensor) A complex tensor.

Return type torch.Tensor

qucumber.utils.cplx.elementwise_mult(x, y)
Alias for scalar_mult().

qucumber.utils.cplx.inner_prod(x, y)

A function that returns the inner product of two complex vectors, x and y (<xly>).

- **x** (torch. Tensor) A complex vector.
- **y** (torch. Tensor) A complex vector.

Raises ValueError – If x and y are not complex vectors with their first dimensions being 2, then the function will not execute.

Returns The inner product, $\langle x|y\rangle$.

Return type torch.Tensor

```
qucumber.utils.cplx.kronecker_prod(x, y)
```

A function that returns the tensor / kronecker product of 2 complex tensors, x and y.

Parameters

- **x** (torch. Tensor) A complex matrix.
- **y** (torch. Tensor) A complex matrix.
- **Raises ValueError** If x and y do not have 3 dimensions or their first dimension is not 2, the function cannot execute.

Returns The tensorproduct of x and y, $x \otimes y$.

Return type torch. Tensor

qucumber.utils.cplx.make_complex(x, y=None)

A function that combines the real (x) and imaginary (y) parts of a vector or a matrix.

Note: x and y must have the same shape. Also, this will not work for rank zero tensors.

Parameters

- **x** (torch. Tensor) The real part
- **y** (*torch.Tensor*) The imaginary part. Can be None, in which case, the resulting complex tensor will have imaginary part equal to zero.

Returns The tensor [x,y] = x + yi.

Return type torch.Tensor

qucumber.utils.cplx.matmul(x, y)

A function that computes complex matrix-matrix and matrix-vector products.

Note: If one wishes to do matrix-vector products, the vector must be the second argument (y).

Parameters

- **x** (torch. Tensor) A complex matrix.
- **y** (torch. Tensor) A complex vector or matrix.

Returns The product between x and y.

Return type torch.Tensor

qucumber.utils.cplx.norm(x)

A function that returns the norm of the argument.

Parameters x (torch. Tensor) – A complex scalar.

Returns |x|.

Return type torch.Tensor

qucumber.utils.cplx.norm_sqr(x)

A function that returns the squared norm of the argument.

Parameters x (torch. Tensor) – A complex scalar.

Returns $|x|^2$.

Return type torch.Tensor

qucumber.utils.cplx.outer_prod(x, y)

A function that returns the outer product of two complex vectors, x and y.

Parameters

- x (torch. Tensor) A complex vector.
- **y** (torch. Tensor) A complex vector.
- **Raises ValueError** If x and y are not complex vectors with their first dimensions being 2, then the function will not execute.

Returns The outer product between x and y, $|x\rangle\langle y|$.

Return type torch.Tensor

qucumber.utils.cplx.scalar_divide(x, y)
A function that computes the division of x by y.

Parameters

- **x** (*torch*. *Tensor*) The numerator (a complex scalar, vector or matrix).
- **y** (*torch*. *Tensor*) The denominator (a complex scalar).

Returns x / y

Return type torch.Tensor

```
qucumber.utils.cplx.scalar_mult(x, y, out=None)
```

A function that computes the product between complex matrices and scalars, complex vectors and scalars or two complex scalars.

Parameters

- **x** (torch. Tensor) A complex scalar, vector or matrix.
- y (torch. Tensor) A complex scalar, vector or matrix.
- **z** (*torch.Tensor*) The complex tensor to write the output to.
- **z** A complex scalar, vector or matrix. Can be None, in which case, a new tensor is created and returned. Otherwise, the method overwrites z.

Returns The product between x and y. Either overwrites z, or returns a new tensor.

Return type torch.Tensor

CHAPTER 13

Data Handling

qucumber.utils.data.extract_refbasis_samples(train_samples, train_bases)
Extract the reference basis samples from the data.

Parameters

- train_samples (numpy.array) The training samples.
- train_bases (numpy.array) The bases of the training samples.

Returns The samples in the data that are only in the reference basis.

Return type torch.tensor

Load the data required for training.

Parameters

- **tr_samples_path** (*str*) The path to the training data.
- **tr_psi_path** (*str*) The path to the target/true wavefunction.
- **tr_bases_path** (*str*) The path to the basis data.
- **bases_path** (*str*) The path to a file containing all possible bases used in the tr_bases_path file.

Returns A list of all input parameters.

Return type list

CHAPTER 14

Indices and tables

- genindex
- modindex
- search

Python Module Index

q

qucumber.utils.cplx,55 qucumber.utils.data,59

Index

Symbols

- __getattr__() (qucumber.callbacks.MetricEvaluator method), 46
- __getattr__() (qucumber.callbacks.ObservableEvaluator method), 47
- __len__() (qucumber.callbacks.MetricEvaluator method), 46
- __len__() (qucumber.callbacks.ObservableEvaluator method), 47

Α

- absolute_value() (in module qucumber.utils.cplx), 55
- amplitude() (qucumber.nn_states.ComplexWaveFunction method), 35
- amplitude() (qucumber.nn_states.WaveFunctionBase method), 39
- apply() (qucumber.observables.NeighbourInteraction method), 53
- apply() (qucumber.observables.SigmaX method), 50
- apply() (qucumber.observables.SigmaY method), 51
- apply() (qucumber.observables.SigmaZ method), 49
- autoload() (qucumber.nn_states.ComplexWaveFunction static method), 35
- autoload() (qucumber.nn_states.PositiveWaveFunction static method), 31
- autoload() (qucumber.nn_states.WaveFunctionBase static method), 39

В

BinaryRBM (class in qucumber.rbm), 29

С

CallbackBase (class in qucumber.callbacks), 43

- clear_history() (qucumber.callbacks.MetricEvaluator method), 46
- clear_history() (qucumber.callbacks.ObservableEvaluator method), 47

ComplexWaveFunction (class in qucumber.nn_s	states), 35
compute_batch_gradients()	(qucum-
ber.nn_states.ComplexWaveFunction	method),
35	
compute_batch_gradients()	(qucum-
ber.nn_states.PositiveWaveFunction 32	method),
compute_batch_gradients()	(qucum-
ber.nn_states.WaveFunctionBase	method),
39	
compute_normalization()	(qucum-
ber.nn_states.ComplexWaveFunction	method),
35	
compute_normalization()	(qucum-
ber.nn_states.PositiveWaveFunction	method),
32	
compute_normalization()	(qucum-
ber.nn_states.WaveFunctionBase	method),
39	
conjugate() (in module qucumber.utils.cplx), 55	

D

device (qucumber.nn_states.ComplexWaveFunction attribute), 36

device (qucumber.nn_states.PositiveWaveFunction attribute), 32

device (qucumber.nn_states.WaveFunctionBase attribute), 39

Е

EarlyStopping (class in qucumber.callbacks), 45 effective_energy() (qucumber.rbm.BinaryRBM method),

29 affective energy gradient() (queumber rhm BineryPBM

effective_energy_gradient() (qucumber.rbm.BinaryRBM method), 29

elementwise_division() (in module qucumber.utils.cplx), 55

elementwise_mult() (in module qucumber.utils.cplx), 55 epochs (qucumber.callbacks.MetricEvaluator attribute), 46

epochs	(qucumber.callbacks.ObservableEvaluator			
	tribute), 47			

extract_refbasis_samples() (in module qucumber.utils.data), 59

F

- fit() (qucumber.nn_states.ComplexWaveFunction method), 36
- fit() (qucumber.nn_states.PositiveWaveFunction method), 32
- fit() (qucumber.nn_states.WaveFunctionBase method), 39

G

generate hilbert space()	(aucum-
born states Complex Weye Eurotion	(quean)
ber.nn_states.Complex waveFunction	method),
36	
generate_hilbert_space()	(qucum-
ber.nn_states.PositiveWaveFunction	method),
32	
generate_hilbert_space()	(qucum-
ber.nn_states.WaveFunctionBase	method),
40	
get_value() (qucumber.callbacks.Metric	Evaluator
method), 47	
get_value() (qucumber.callbacks.Observable	Evaluator
method), 48	
gibbs_steps() (qucumber.rbm.BinaryRBM meth	10d), 29
gradient() (qucumber.nn_states.ComplexWav	eFunction
method), 36	
gradient() (qucumber.nn_states.PositiveWav	eFunction
method), 33	
gradient() (qucumber.nn_states.WaveFun	ctionBase

method), 40

I

initialize_parameters() (qucumber.rbm.BinaryRBM method), 29

inner_prod() (in module qucumber.utils.cplx), 55

K

kronecker_prod() (in module qucumber.utils.cplx), 56

L

LambdaCallback (class in qucumber.callbacks), 44

- load() (qucumber.nn_states.ComplexWaveFunction method), 37
- load() (qucumber.nn_states.PositiveWaveFunction method), 33
- load() (qucumber.nn_states.WaveFunctionBase method), 40

load_data() (in module qucumber.utils.data), 59 Logger (class in qucumber.callbacks), 44

Μ

```
make_complex() (in module qucumber.utils.cplx), 56
matmul() (in module qucumber.utils.cplx), 56
max_size
           (qucumber.nn states.ComplexWaveFunction
         attribute). 37
max size (qucumber.nn states.PositiveWaveFunction at-
         tribute). 33
max size
                (qucumber.nn_states.WaveFunctionBase
         attribute), 41
MetricEvaluator (class in qucumber.callbacks), 46
ModelSaver (class in qucumber.callbacks), 44
Ν
name (qucumber.observables.NeighbourInteraction at-
         tribute), 53
name (qucumber.observables.SigmaX attribute), 50
name (qucumber.observables.SigmaY attribute), 52
name (qucumber.observables.SigmaZ attribute), 49
names (qucumber.callbacks.MetricEvaluator attribute),
         47
         (qucumber.callbacks.ObservableEvaluator
names
                                                   at-
         tribute), 48
NeighbourInteraction (class in qucumber.observables), 53
networks
           (qucumber.nn_states.ComplexWaveFunction
         attribute), 37
networks (qucumber.nn_states.PositiveWaveFunction at-
         tribute), 33
networks
                (qucumber.nn states.WaveFunctionBase
         attribute), 41
norm() (in module qucumber.utils.cplx), 56
norm_sqr() (in module qucumber.utils.cplx), 57
Ο
ObservableEvaluator (class in qucumber.callbacks), 47
on_batch_end()
                     (qucumber.callbacks.CallbackBase
         method), 43
on_batch_start()
                     (qucumber.callbacks.CallbackBase
         method), 43
```

on_epoch_end() (qucumber.callbacks.CallbackBase method), 43

on_epoch_start() (qucumber.callbacks.CallbackBase method), 43

- on_train_end() (qucumber.callbacks.CallbackBase method), 44
- on_train_start() (qucumber.callbacks.CallbackBase method), 44
- outer_prod() (in module qucumber.utils.cplx), 57

Ρ

partition() (qucumber.rbm.BinaryRBM method), 30

- phase() (qucumber.nn_states.ComplexWaveFunction method), 37
- phase() (qucumber.nn_states.PositiveWaveFunction method), 33

- phase() (qucumber.nn_states.WaveFunctionBase method), 41
- PositiveWaveFunction (class in qucumber.nn_states), 31
- prob_h_given_v() (qucumber.rbm.BinaryRBM method), 30
- prob_v_given_h() (qucumber.rbm.BinaryRBM method), 30
- probability() (qucumber.nn_states.ComplexWaveFunction method), 37
- probability() (qucumber.nn_states.PositiveWaveFunction method), 33
- probability() (qucumber.nn_states.WaveFunctionBase method), 41
- psi() (qucumber.nn_states.ComplexWaveFunction method), 37
- psi() (qucumber.nn_states.PositiveWaveFunction method), 34
- psi() (qucumber.nn_states.WaveFunctionBase method), 41

Q

qucumber.utils.cplx (module), 55 qucumber.utils.data (module), 59

R

rbm_am (qucumber.nn_states.ComplexWaveFur	nction at-			
tribute), 38				
rbm_am (qucumber.nn_states.PositiveWaveFun	ction at-			
tribute), 34				
rbm_am (qucumber.nn_states.WaveFunctionB	ase at-			
tribute), 41				
rbm_ph (qucumber.nn_states.ComplexWaveFun	ction at-			
tribute), 38				
reinitialize_parameters() (qucum				
ber.nn_states.ComplexWaveFunction	method),			
38				
reinitialize_parameters()	(qucum-			
ber.nn_states.PositiveWaveFunction	method),			
34				
reinitialize_parameters()	(qucum-			
ber.nn_states.WaveFunctionBase	method),			
41				
S				

sample()	(qucu	mber.nı	n_states.	.Cor	nple	xWav	veFu	nction
	method)	, 38						
	,			-			-	

- sample() (qucumber.nn_states.PositiveWaveFunction
 method), 34
- sample() (qucumber.nn_states.WaveFunctionBase method), 41
- sample() (qucumber.observables.NeighbourInteraction method), 53
- sample() (qucumber.observables.SigmaX method), 50
- sample() (qucumber.observables.SigmaY method), 52

sample() (qucumber.observ	ables.SigmaZ metho	d), 49
sample_h_given_v()	(qucumber.rbm.Bin	naryRBM
method), 30		
sample_v_given_h()	(qucumber.rbm.Bi	naryRBM
method), 30		•
save() (qucumber.nn	states.ComplexWave	Function
method), 38	- 1	
save() (qucumber.nr	states PositiveWave	Function
method) 34		
save() (queumber nn_states	WaveFunctionBase	method)
41	. Waver unetionDuse	method),
scalar divide() (in module	aucumber utils coly)	57
scalar mult() (in module qu	(ucumber utils only)	, <i>51</i>
SigmaX (alass in quaumbar	r observables) 50) /
SigmaX (class in queumber	nobservables), 50	
Signa F (class in queumber	.observables), 51	
SigmaZ (class in qucumber	observables), 49	, , .
statistics() (qucumber.obs	ervables.Neighbourli	nteraction
method), 53	11 01 17 1	1) 54
statistics() (qucumber.obser	vables.SigmaX meth	100, 51
statistics() (qucumber.obser	vables.SigmaY meth	10d), 52
statistics() (qucumber.obser	vables.SigmaZ meth	od), 50
statistics_from_samples()		(qucum-
ber.observables.N	JeighbourInteraction	method),
54		
statistics_from_samples()		(qucum-
ber.observables.S	igmaX method), 51	
<pre>statistics_from_samples()</pre>		(qucum-
ber.observables.S	igmaY method), 52	
statistics from samples()		(qucum-
ber.observables.S	igmaZ method), 50	1
stop training (qucumber.nn	states.ComplexWay	Function
attribute). 38		
stop training (queumber.nr	states PositiveWave	Function
attribute) 34		or unction
stop_training (aucumber nn	states WaveFunctio	nBase at-
tribute) 42	_states. Waver unerio	iiiDase at
subspace vector()		(aucum
bernn states Cor	mplayWayaFunction	(queum-
	inplex waver unction	method),
Jo subspace vector()		(0)0000
subspace_vector()	iting Ways From ating	(qucum-
per.nn_states.Pos	nive wavefunction	methoa),
54		1
subspace vector()		(qucum-

- ber.nn_states.WaveFunctionBase method), 42
- symbol (qucumber.observables.NeighbourInteraction attribute), 54
- symbol (qucumber.observables.SigmaX attribute), 51

symbol (qucumber.observables.SigmaY attribute), 52 symbol (qucumber.observables.SigmaZ attribute), 50

Т

Timer (class in qucumber.callbacks), 48

V

VarianceBasedEarlyStopping (class in qucumber.callbacks), 45

W

WaveFunctionBase (class in qucumber.nn_states), 39